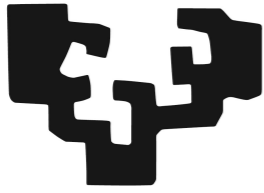


eman ta zabal zazu



Universidad  
del País Vasco

Euskal Herriko  
Unibertsitatea



ZTF-FCT

# **CHASING MONOPOLES**

**A. LOPEZ-EIGUREN (UPV-EHU)**

(**IberiCOS 2015**, Aranjuez)

# OUTLINE

- Global Monopole Networks
- Velocities
- Results
- Applications

# GLOBAL MONOPOLES

$$\mathcal{S} = \int d^4x \left[ \frac{1}{2} \partial_\mu \Phi^i \partial^\mu \Phi^i - \frac{\lambda}{4} (|\Phi|^2 - \eta^2)^2 \right]$$

$$i = 1, 2, 3; \quad |\Phi| \equiv \sqrt{\Phi^i \Phi^i}$$

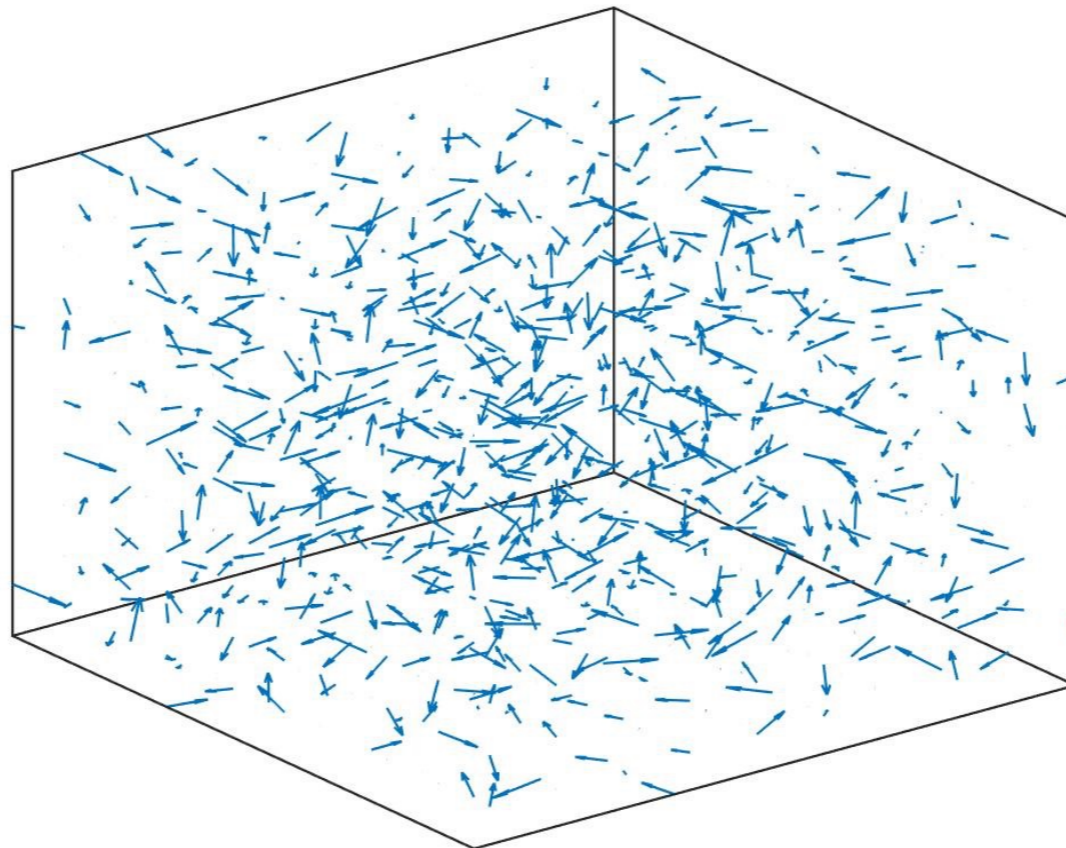
- O(3) symmetry spontaneously broken to O(2)
- Topological charge can be used to detect monopoles

$$N = \frac{1}{8\pi} \oint dS^{ij} |\Phi|^{-3} \epsilon_{abc} \Phi^a \partial_i \Phi^b \partial_j \Phi^c$$



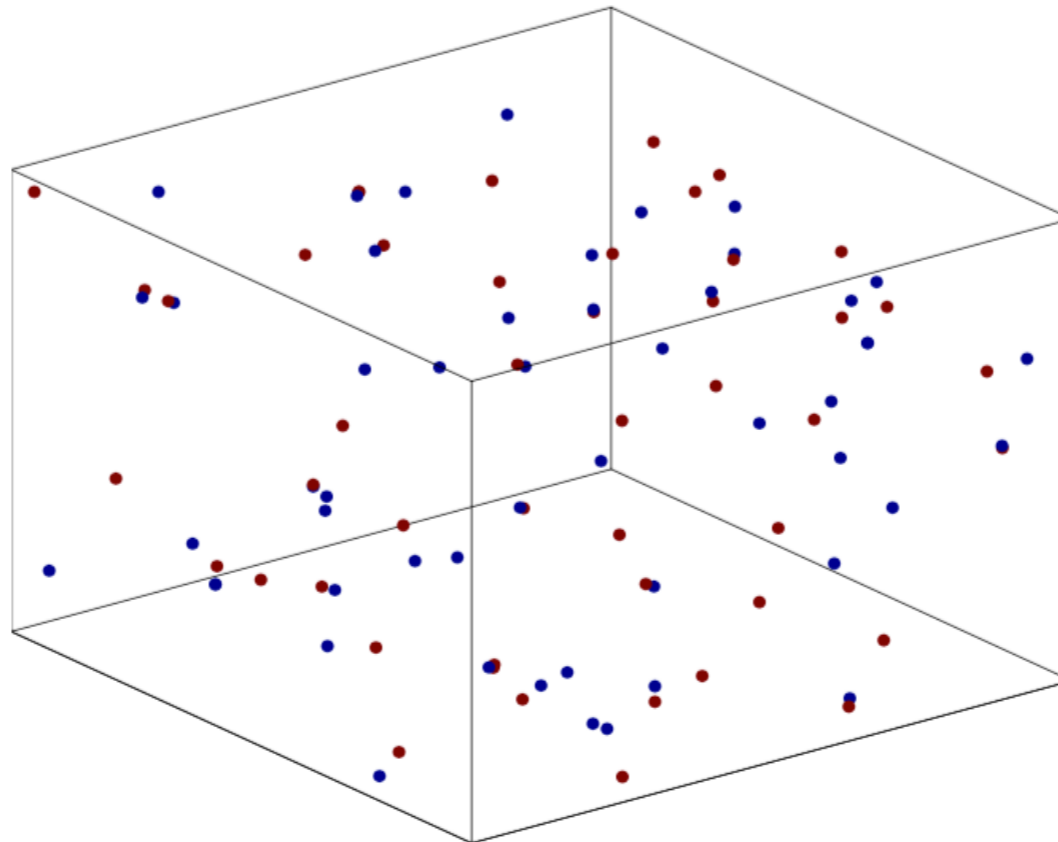
# FIELD THEORY SIMULATIONS

- $2048^3$  lattices in radiation and matter eras in expanding universe
- Discretised e.o.m. are evolved in the lattice



# FIELD THEORY SIMULATIONS

- $2048^3$  lattices in radiation and matter eras in expanding universe
- Discretised e.o.m. are evolved in the lattice



# VELOCITIES

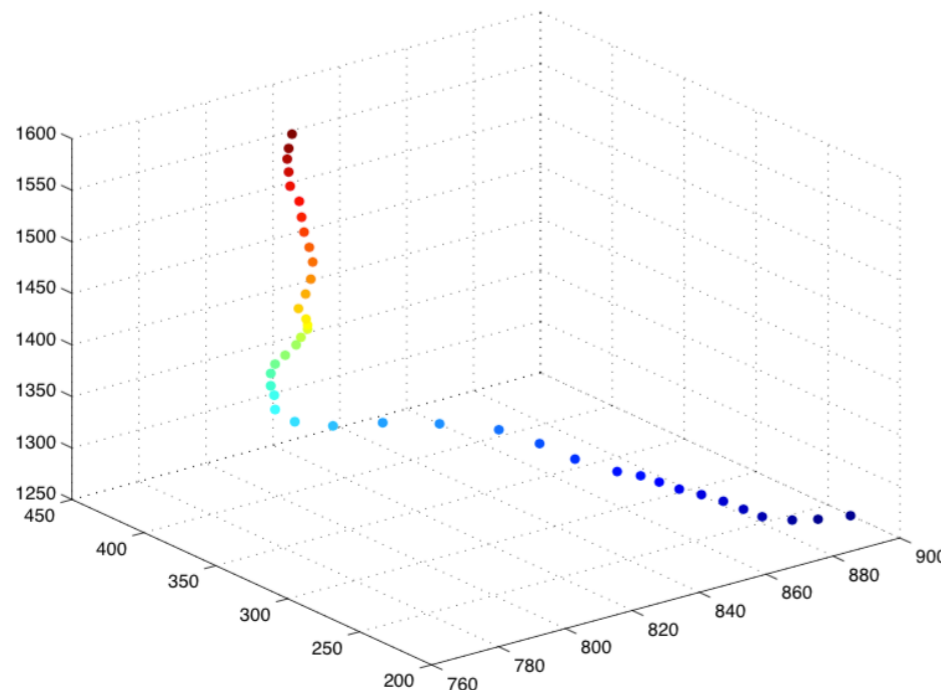
- Averaging method:

**Stuckey et al.** [10.1103/PhysRevD.79.123504](https://arxiv.org/abs/0812.1929) [arXiv:0812.1929](https://arxiv.org/abs/0812.1929)

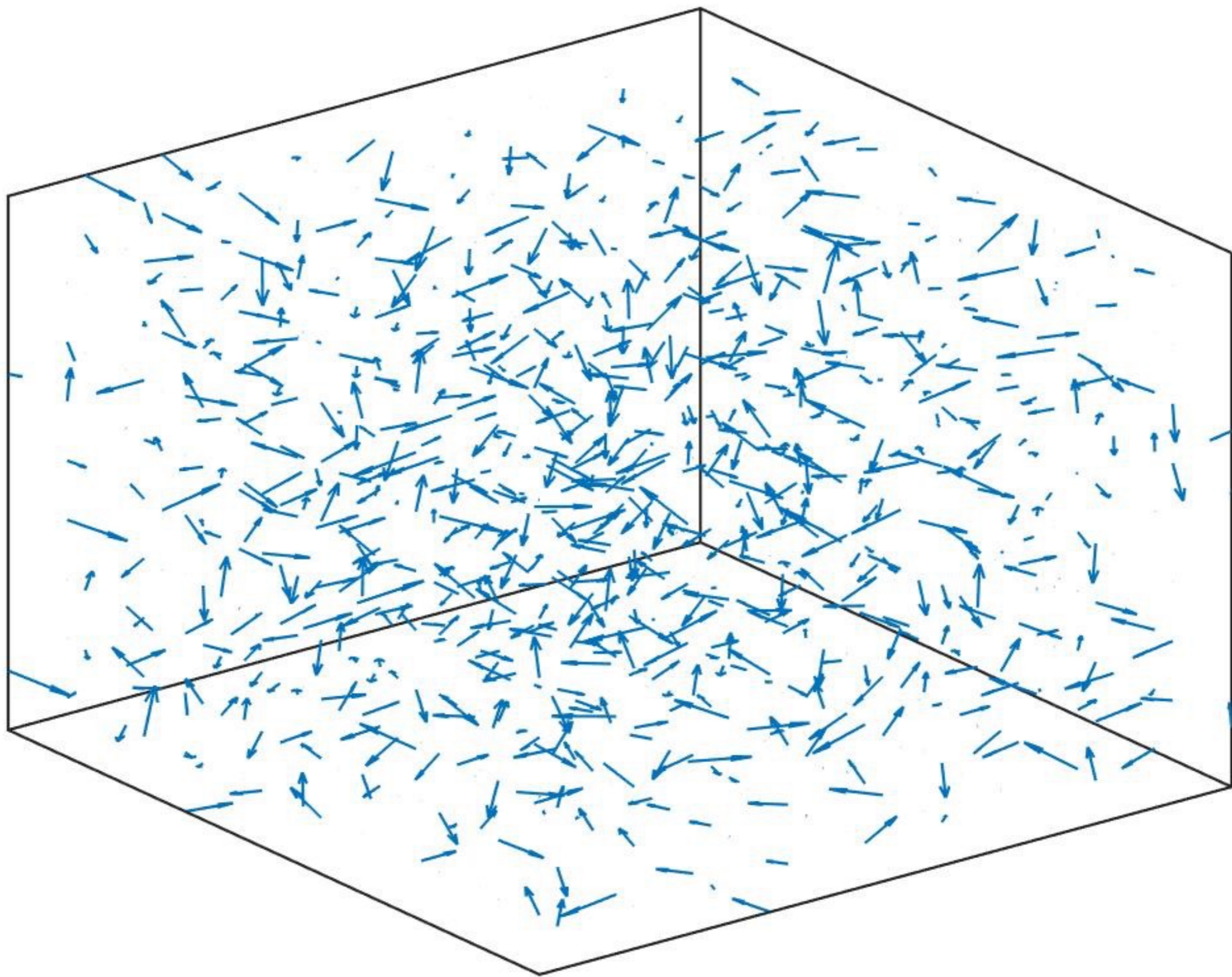
$$\gamma^2 \langle \dot{x}^2 \rangle = \frac{(\Pi^i)^2}{(\partial\Phi^i)^2}$$

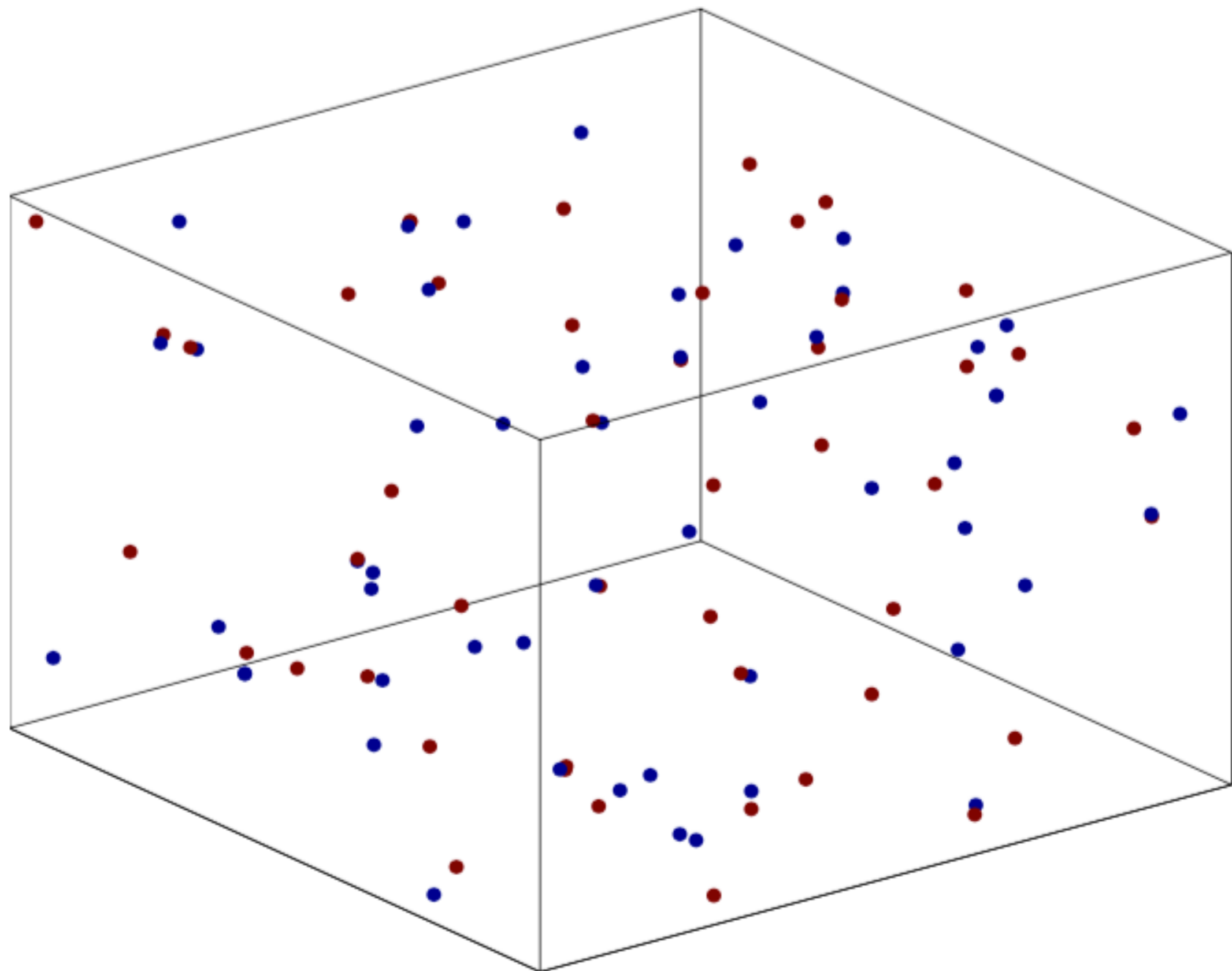
$$\Pi^i = \dot{\Phi}^i \quad \partial\Phi^i = \frac{\partial\Phi^i}{\partial\vec{x}}$$

- Monopole tracking method:

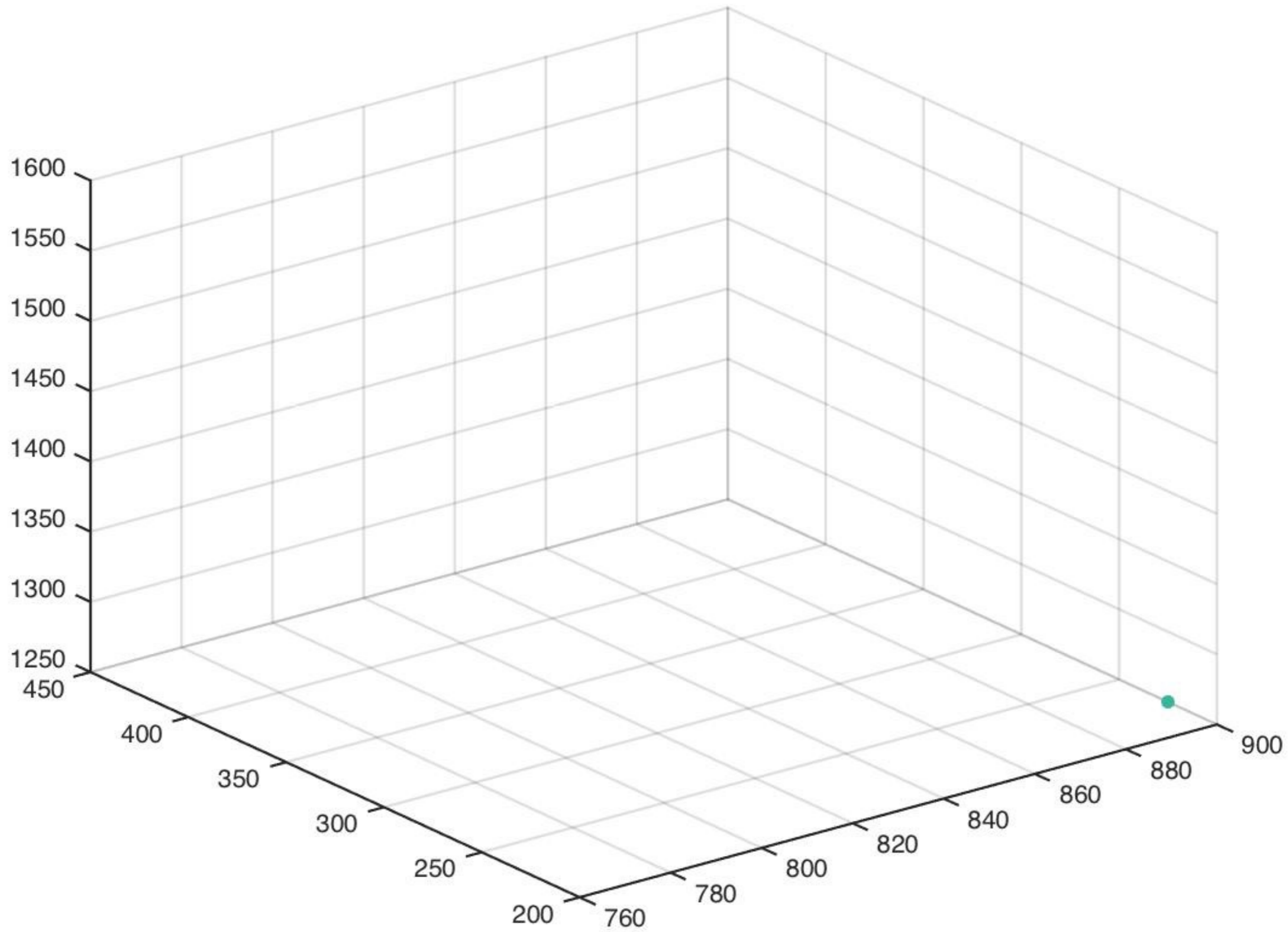


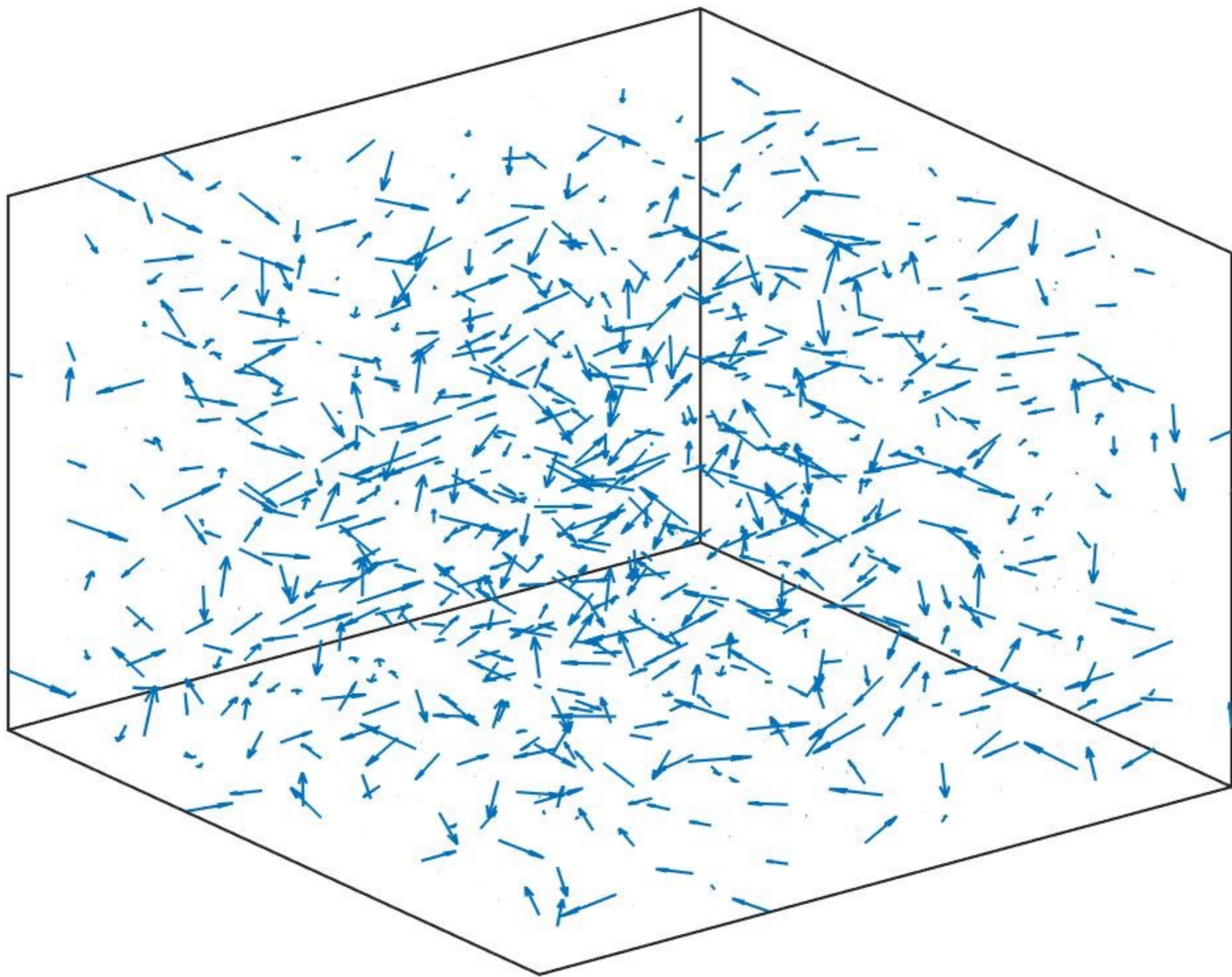
$$v_m = \frac{\Delta d}{\Delta t}$$

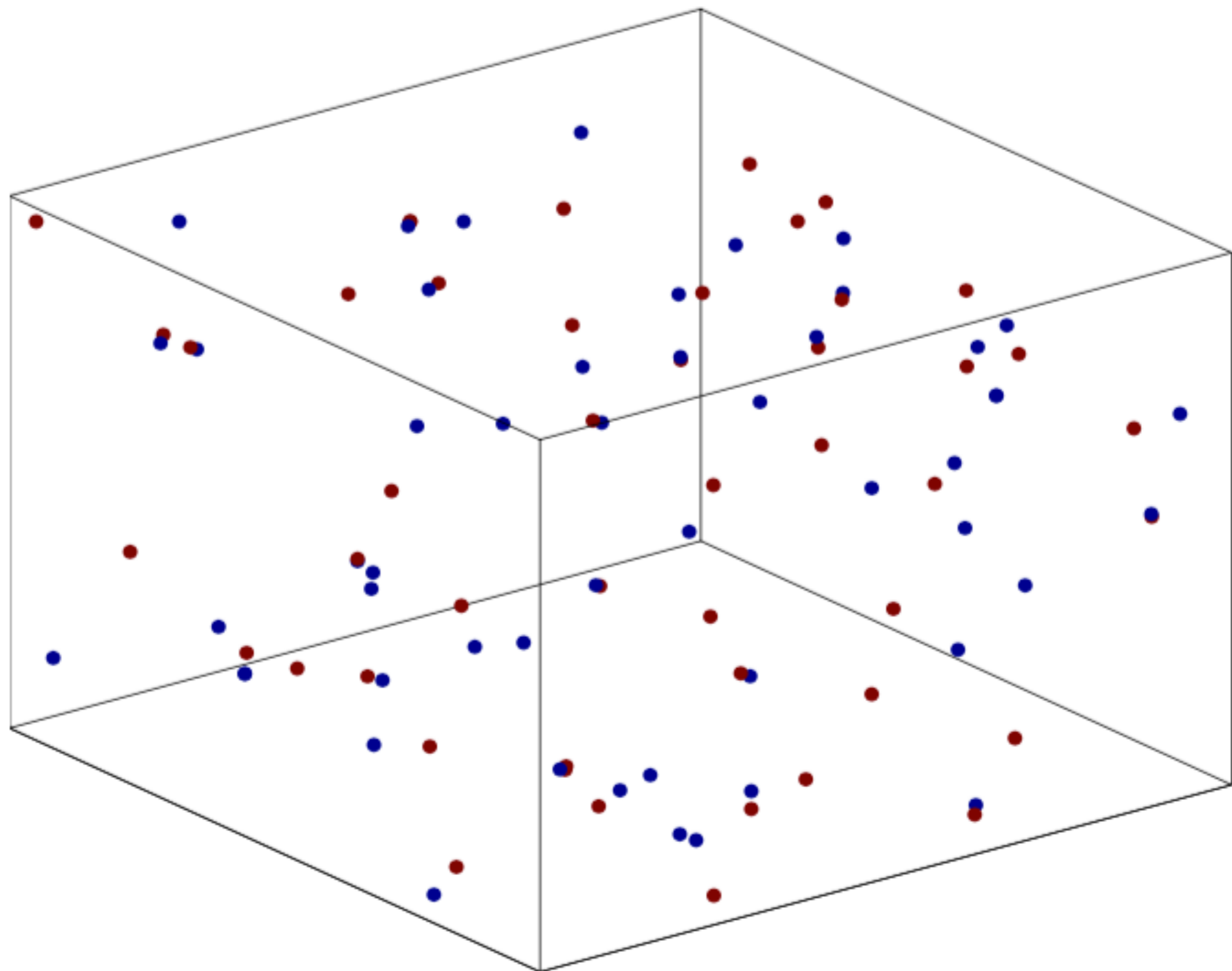


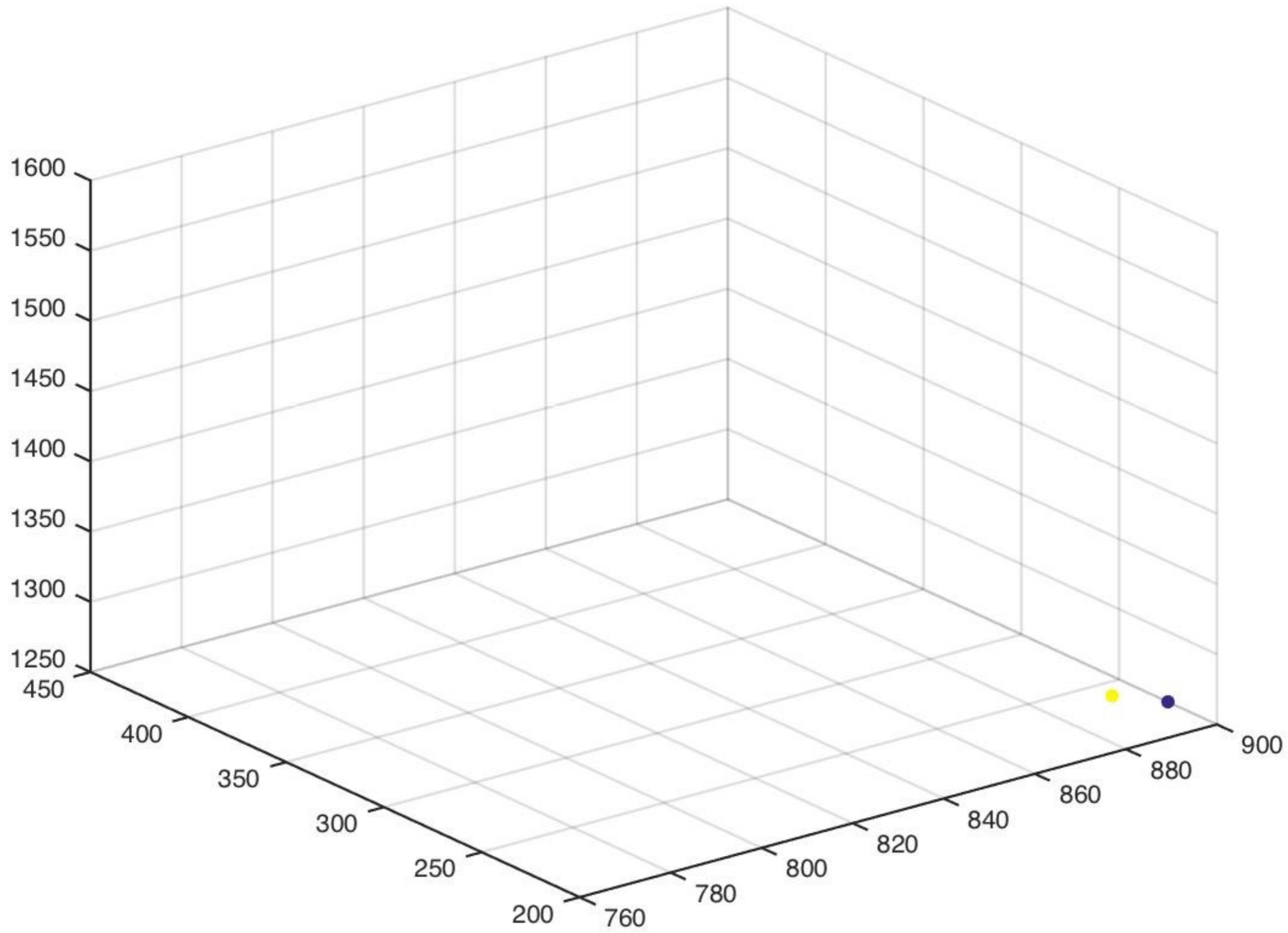


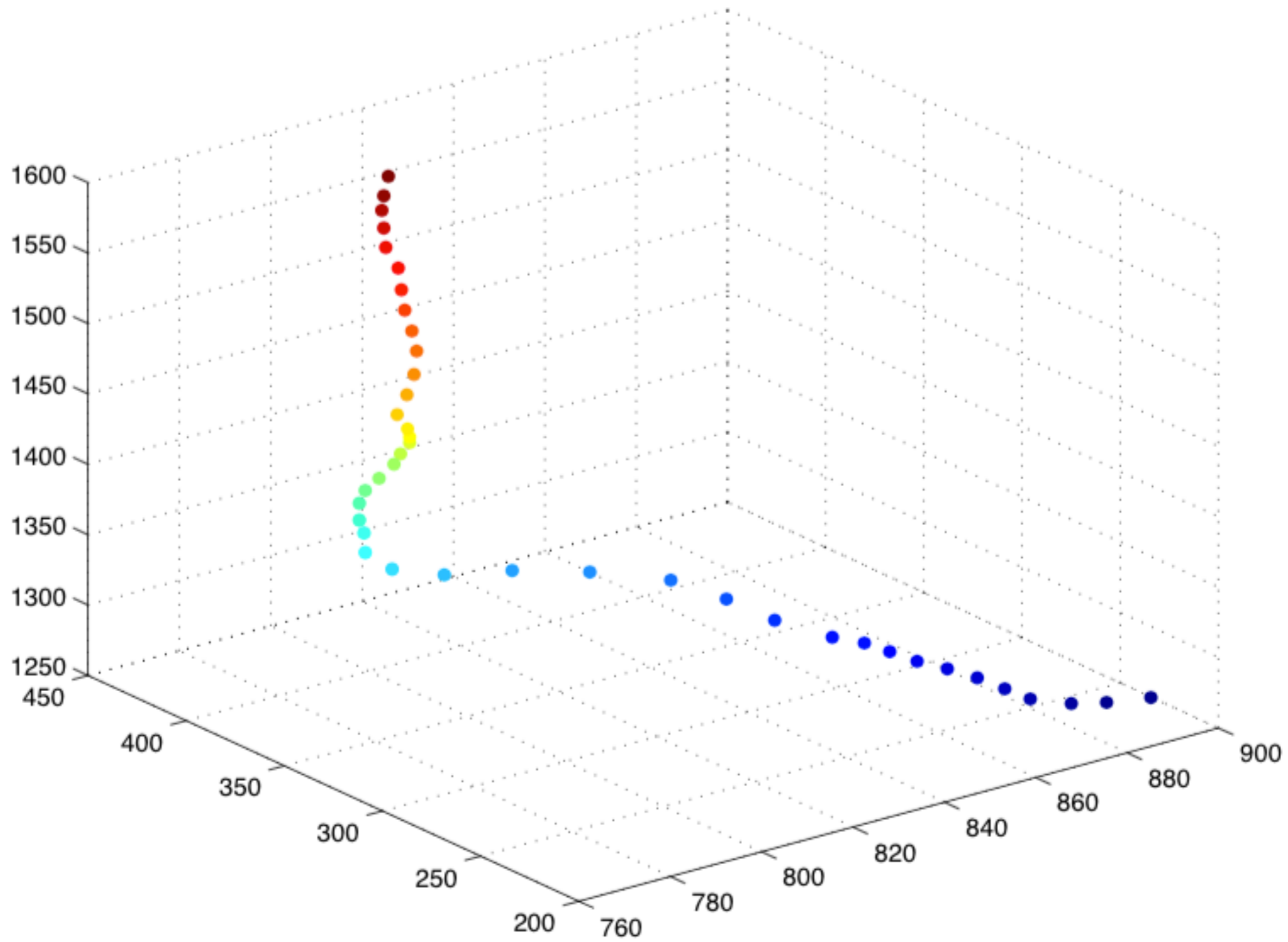




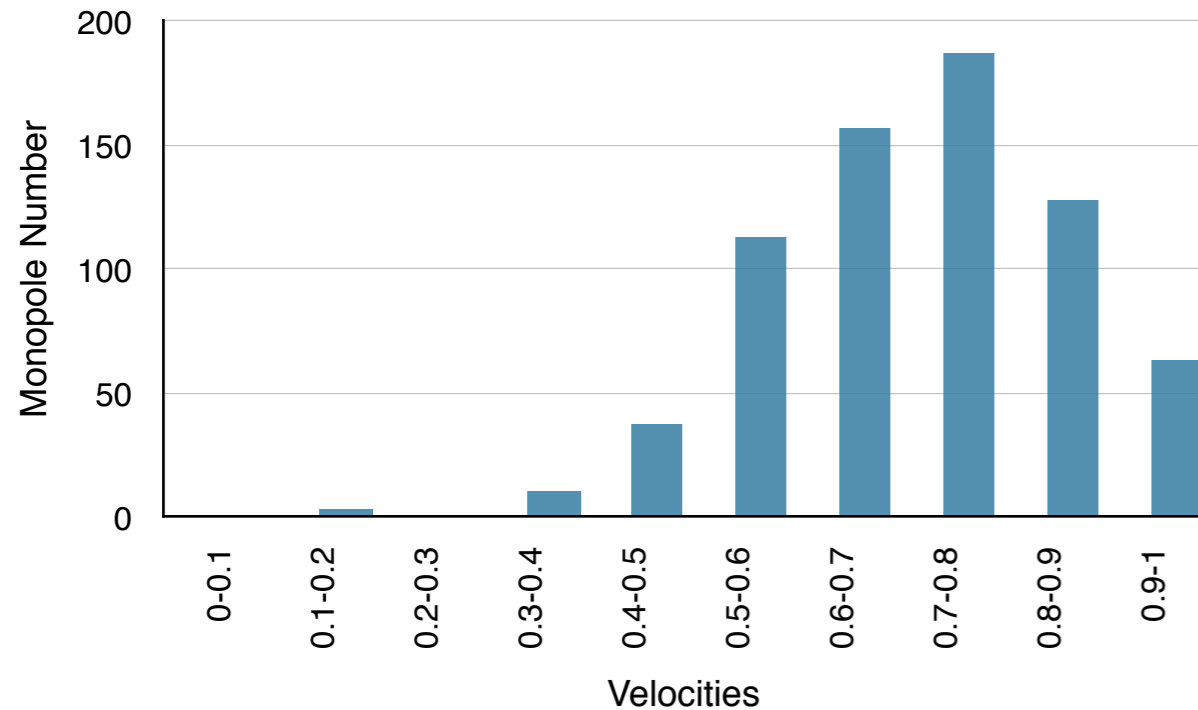








# RESULTS



	Track	Averaging
Radiation	$0.704 \pm 0.002$	$0.702 \pm 0.001$
Matter	$0.619 \pm 0.002$	$0.64 \pm 0.02$

- Overall network velocity can be computed
- The history of each monopole can be followed:
  - Instantaneous velocities
  - Much more information than average network properties
- Our new method confirms the validity of the Averaging method
- The monopole network properties have been characterised better

# APPLICATIONS

- Our results are necessary to calibrate parameters of analytic models:
  - Global Monopoles
  - Semilocal Strings:

**Achúcarro, Avgoustidis, Leite, ALE, Martins, Nunes and Urrestilla**

**-arXiv:1312.2123 10.1103/PhysRevD.89.063503**

**-arXiv: 15MM.XXXX**

**-arXiv:15MM.XXX**

**THANK YOU!!!**



